## Virtual Learning

 PhysicsHooke's Law Simulation Part II April 30, 2020

## Physics

## Hooke's Law Simulation Part II: April 30,2020

## Objective/Learning Target:

Students will use a computer simulation to examine Hooke's Law.

## Quick Review \#1

Two smooth balls of exactly the same size, one made of wood and the other of iron, are dropped from a high building to the ground below. The ball to encounter the greater force of air resistance on the way down is the
a) Wooden ball
b) Iron ball
c) Both the same

## Quick Review \#1 Answer

## Air resistance depends on both the size and speed of a

 falling object. Both balls have the same size, but the heavier iron ball falls faster through the air and encounters more air resistance in its fall.

Quick Review \#2
Why does a cat that accidentally falls from the top of a 50 -story building hit a safety net below no faster than if it fell from the 20th story?

## Quick Review \#2 Answer

The cat reaches terminal velocity just around 20 stories, so the additional fall from 50 stories wouldn't result in a faster velocity for the cat.


## Hooke's Law Part II

## Introduction

You will use a computer simulation today to investigate Hooke's Law.
Since this is "inquiry based", you're not supposed to know everything going in, but learn as we walk through the lesson. You must read the following slides carefully. Let's get started!

## Hooke's Law Part II

## Website: Hooke's Law Simulation

Make sure to use the HTML5 version.
Select the Systems icon and double click to start. Hooke's Law


Intro


Systems

## Hooke's Law Part II

Select the options 'Displacement', 'Equilibrium Potion’ and 'Values'. Make sure the option of two springs in parallel is selected so that the springs look like the setup in the image below.



## Hooke's Law Part II

1. Keep the top spring constant $k_{T}=200 \mathrm{~N} / \mathrm{m}$ and the bottom spring constant $k_{B}=200 \mathrm{~N} / \mathrm{m}$. Apply 100 N of force to the right.
2. Measure the extension and determine the total spring constant of the two springs in parallel (Force/extension). Record the results in the data table.
3. Repeat steps $1 \& 2$ three more times by changing the values of the spring constants. Be sure to select some constants that are not equal. Record the results in the table.

| $k_{T}$ | $k_{\mathrm{B}}$ | $F$ | Ext | $k_{\text {tot }}$ |
| :---: | :---: | :---: | :---: | :---: |
| $(\mathrm{N} / \mathrm{m})$ | $(\mathrm{N} / \mathrm{m})$ | $(\mathrm{N})$ | $(\mathrm{m})$ | $(\mathrm{N} / \mathrm{m})$ |
|  |  | 100 |  |  |
|  |  | 100 |  |  |
|  |  | 100 |  |  |
|  |  | 100 |  |  |

Hooke's Law Part II
Describe the relationship between the individual spring constants $k_{T}$ and $k_{B}$, and the total spring constant for springs in parallel.

Try to write this in the form of an equation.


## Hooke's Law Part II

Press the series spring button so that the springs change their combination to look like the setup in the image below:


## Hooke's Law Part II

1. Keep the left spring constant $k L=400 \mathrm{~N} / \mathrm{m}$ and the right spring constant $k_{R}=400 \mathrm{~N} / \mathrm{m}$. Apply 100 N of force to the right.
2. Measure the extension and determine the total spring constant of the two springs in series (Force/extension). Record the results in the data table.
3. Repeat steps $1 \& 2$ three more times by changing the values of the spring constants. Be sure to select some constants that are not equal. Record the results in the table.

| $k_{L}$ | $k_{R}$ | $F$ | Ext | $k_{\text {tot }}$ |
| :---: | :---: | :---: | :---: | :---: |
| $(\mathrm{N} / \mathrm{m})$ | $(\mathrm{N} / \mathrm{m})$ | $(\mathrm{N})$ | $(\mathrm{m})$ | $(\mathrm{N} / \mathrm{m})$ |
|  |  | 100 |  |  |
|  |  | 100 |  |  |
|  |  | 100 |  |  |
|  |  | 100 |  |  |

## Hooke's Law Part II

Three students offer a model for finding the total spring constant for two springs in series:

Student 1: $k_{\text {tot }}=\underline{k_{L}}+k_{B}$ $k_{1} k_{R}$

Student 2: $k_{\text {tot }}=\left(\underline{k}+k_{R}\right)^{2}$ $k_{L}+k_{R}$

Student 3: $\frac{1}{k_{\text {tot }}}=\frac{1}{k_{L}}+\frac{1}{k_{R}}$.
Explain which student's model is correct based on your results.

## Hooke's Law Part II Answer

For a single spring we know

$$
F_{\mathrm{tot}}=k x
$$

The relationship for two springs in parallel:

$$
\begin{aligned}
\mathrm{F}_{\mathrm{tot}} & =k_{1} \mathrm{x}+k_{2} \mathrm{x} \\
& =\left(k_{1}+k_{2}\right) \mathrm{x}
\end{aligned}
$$

The total spring constant is equal to the sum of the individual spring

| $k_{T}$ | $k_{B}$ | $F$ | Ext | $k_{\text {tot }}$ |
| :---: | :---: | :---: | :---: | :---: |
| $(\mathrm{N} / \mathrm{m})$ | $(\mathrm{N} / \mathrm{m})$ | $(\mathrm{N})$ | $(\mathrm{m})$ | $(\mathrm{N} / \mathrm{m})$ |
| 200 | 200 | 100 | 0.250 | 400 |
| 200 | 400 | 100 | 0.167 | 599 |
| 400 | 600 | 100 | 0.100 | 1000 |
| 200 | 600 | 100 | 0.125 | 800 |

1: $k_{\text {tot }}=\underline{k_{L}+k_{R}} \frac{k_{L}}{k_{L} k_{R}}=\frac{400+400}{400 \times 400}=0.005$

2: $k_{\text {tot }}=\left(\underline{k_{L}}+k_{R}\right)^{2}=(400+400)^{2}=800$ $k_{L}+k_{R} \quad 400+400$

3: $\frac{1}{k_{\text {tot }}}=\frac{1}{k_{L}}+\frac{1}{k_{R}}=\frac{1}{400}+\frac{1}{400}=200$

Plugging in the first set of values into each equation yielded the results above. Only Student 3 had the right relationship, as the two $400 \mathrm{~N} / \mathrm{m}$ springs resulted in a $k$ tot of $200 \mathrm{~N} / \mathrm{m}$.

| $k_{L}$ | $k_{R}$ | $F$ | $E x t$ | $k_{\text {tot }}$ |
| :---: | :---: | :---: | :---: | :---: |
| $(\mathrm{N} / \mathrm{m})$ | $(\mathrm{N} / \mathrm{m})$ | $(\mathrm{N})$ | $(\mathrm{m})$ | $(\mathrm{N} / \mathrm{m})$ |
| 400 | 400 | 100 | 0.500 | 200 |
| 200 | 400 | 100 | 0.750 | 133 |
| 600 | 400 | 100 | 0.417 | 240 |
| 200 | 600 | 100 | 0.667 | 150 |

## Additional Practice

Return to the simulation and use the equations to solve for different spring constants and
then check your answers using the simulation.

